

Section 7.2 and 7.3 – Check your Understanding

Given a point on the terminal side of angle θ . Evaluate the three trigonometric functions of θ

1. $(3, 7)$

$$\begin{aligned} 3^2 + 7^2 &= r^2 \\ 9 + 49 &= r^2 \\ 58 &= r^2 \\ r &= \sqrt{58} \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{7}{\sqrt{58}} \\ \cos \theta &= \frac{3}{\sqrt{58}} \end{aligned}$$

$$\tan \theta = \frac{7}{3}$$

2. $-\sqrt{17}, -2\sqrt{2}$

$$\begin{aligned} (-\sqrt{17})^2 + (-2\sqrt{2})^2 &= r^2 \\ 17 + 8 &= r^2 \\ r^2 &= 25 \quad r = 5 \end{aligned}$$

$$\sin \theta = -\frac{2\sqrt{2}}{5}$$

$$\cos \theta = -\frac{\sqrt{17}}{5}$$

$$\tan \theta = \frac{2\sqrt{2}}{\sqrt{17}}$$

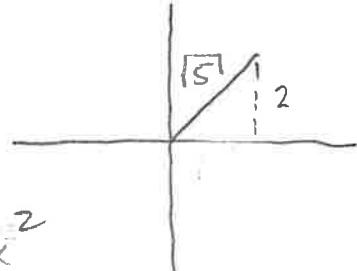
Given one of three primary trigonometric functions, find the other two trigonometric function of θ

3. $\sin \theta = \frac{2}{\sqrt{5}}$ θ is in Q1

$$r^2 - y^2 = x^2$$

$$\sqrt{5}^2 - 2^2 = x^2$$

$$5 - 4 = x^2$$



$$\tan \theta = 2$$

$$\cos \theta = \frac{1}{\sqrt{5}}$$

4. $\tan \theta = -\frac{2}{\sqrt{21}}$ θ is in Q2

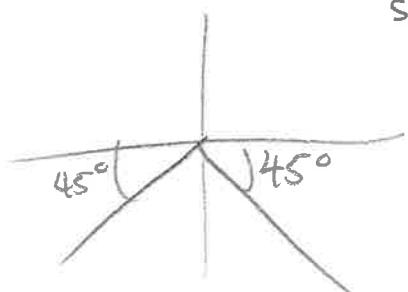
$$\begin{aligned} 2^2 + (-\sqrt{21})^2 &= r^2 \\ 4 + 21 &= r^2 \\ r^2 &= 25 \\ r &= 5 \end{aligned}$$

$$\sin \theta = \frac{3}{5}$$

$$\cos \theta = -\frac{\sqrt{21}}{5}$$

Find all angles, $0^\circ \leq \theta < 360^\circ$, that satisfy each equation, use special angles and give exact answers, not decimals

5. $\sin \theta = -\frac{1}{\sqrt{2}}$



45° ref angle

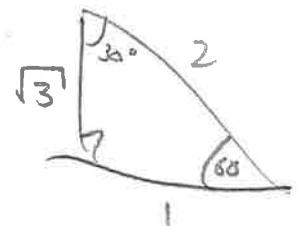
\sin neg in
Q3 Q4

Q3 $\theta = 180 + 45^\circ$
 $\theta = 225^\circ$

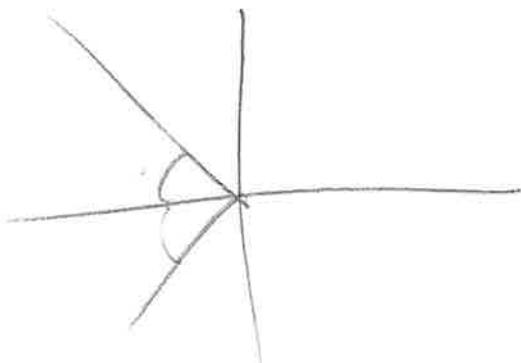
Q4 $\theta = 360 - 45^\circ$
 $\theta = 315^\circ$

$\cos \theta = -\frac{\sqrt{3}}{2}$

ref angle:



\cos neg in Q2 and Q3



Q2 : $180 - 30^\circ$

$\theta = 150^\circ$

Q3 : $180 + 30^\circ$

$\theta = 210^\circ$