

Exercise 1 – Practice Problems

1. Express the interval as an inequality in set notation and graph the inequality on the number line.

a) $(-2, 6)$

$$\{x | x \in \mathbb{R}, -2 < x < 6\}$$



b) $[-3, -2)$

$$\{x | x \in \mathbb{R}, -3 \leq x < -2\}$$



c) $(1, 4]$

$$\{x | x \in \mathbb{R}, 1 < x \leq 4\}$$



d) $[-2, 1.5]$

$$\{x | x \in \mathbb{R}, -2 \leq x \leq 1.5\}$$



e) $[3, \infty)$

$$\{x | x \in \mathbb{R}, x \geq 3\}$$



f) $(-\infty, 2)$

$$\{x | x \in \mathbb{R}, x < 2\}$$



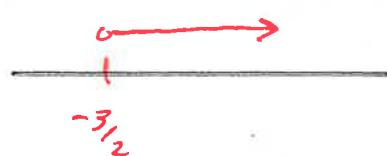
g) $(-\infty, 1]$

$$\{x | x \in \mathbb{R}, x \leq 1\}$$



h) $(-\frac{3}{2}, \infty)$

$$\{x | x \in \mathbb{R}, x > -\frac{3}{2}\}$$



2. Express the inequality in interval notation and graph the interval on a number line.

a) $x < 2$

$$(-\infty, 2)$$



b) $0 < x < 3$

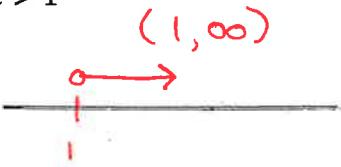
$$(0, 3)$$



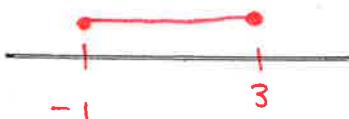
c) $-1 \leq x < 2$ $[-1, 2)$



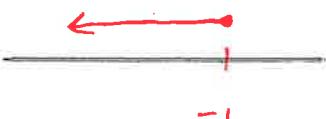
d) $x > 1$ $(1, \infty)$



e) $-1 \leq x \leq 3$ $[-1, 3]$



f) $x \leq -1$ $(-\infty, -1]$

**Exercise 2 – Practice Problems**

1. Solve the inequality.

a) $3x + 7 > 0$

$$\boxed{x > -\frac{7}{3}}$$

$$(-\frac{7}{3}, \infty)$$

b) $18 - 4x < 0$

$$-4x < -18$$

$$\boxed{x > \frac{9}{2}}$$

$$(\frac{9}{2}, \infty)$$

c) $17 - 2x \geq 13$

$$-2x \geq -4$$

$$\boxed{x \leq 2}$$

$$(-\infty, 2]$$

d) $2x + 1 < 5x - 11$

$$12 < 3x$$

$$\boxed{4 < x}$$

$$(4, \infty)$$

e) $2x - 1 < 19$

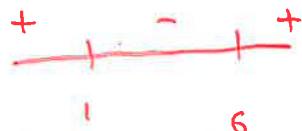
$$2x < 20$$

$$\boxed{x < 10}$$

$$(-\infty, 10)$$

f) $x^2 - 7x + 6 > 0$

$$(x-1)(x-6) > 0$$



$$\{x | x \in \mathbb{R}, x < 1 \text{ or } x > 6\}$$

g) $12 - x - x^2 > 0$

$$\begin{aligned}x^2 + x - 12 &< 0 \\(x+4)(x-3) &< 0\end{aligned}$$

$\begin{array}{c}+ \quad - \quad + \\ \hline -4 \quad 3\end{array}$

$$\begin{aligned}\{x | x \in \mathbb{R}, -4 < x < 3\} \\(-4, 3)\end{aligned}$$

i) $x^2 - 9 > 0$

$(x+3)(x-3) > 0$

$$\begin{array}{c}+ \quad - \quad + \\ \hline -3 \quad 3\end{array}$$

$$\begin{aligned}\{x | x \in \mathbb{R}, x < -3 \text{ or } x > 3\} \\(-\infty, -3) \cup (3, \infty)\end{aligned}$$

k) $(x+1)(2x+1)(x-6) > 0$

$$\begin{array}{c}- \quad + \quad - \quad + \\ \hline -1 \quad -\frac{1}{2} \quad 6\end{array}$$

$$\begin{aligned}\{x | x \in \mathbb{R}, -1 < x < -\frac{1}{2} \text{ or } x > 6\} \\(-1, -\frac{1}{2}) \cup (6, \infty)\end{aligned}$$

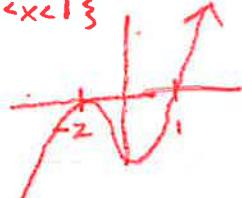
m) $x^3 + 3x^2 - 4 < 0$

$$\begin{aligned}x-1 &\cancel{|} \frac{x^2 + 4x + 4}{x^2 + 3x^2 + 0x - 4} \\&\cancel{|} \frac{x^3 - x^2}{4x^2 + 0x} \\&\cancel{|} \frac{4x^2 - 4x}{4x - 4} \\&\cancel{|} \frac{4x - 4}{0}\end{aligned}$$

$\begin{array}{c}+ \quad - \quad + \\ \hline -1 \quad 0\end{array}$

$$\{x | x \in \mathbb{R}, x < -2 \text{ or } -2 < x < 1\}$$

$(-\infty, -2) \cup (-2, 1)$



h) $x^2 < 3x$

$$\begin{aligned}x^2 - 3x &< 0 \\x(x-3) &< 0\end{aligned}$$

$\begin{array}{c}+ \quad - \quad + \\ \hline 0 \quad 3\end{array}$

$$\begin{aligned}\{x | x \in \mathbb{R}, 0 < x < 3\} \\(0, 3)\end{aligned}$$

j) $x^2 \leq 5$

$x^2 - 5 \leq 0$

$$(x - \sqrt{5})(x + \sqrt{5}) \leq 0$$

$\begin{array}{c}+ \quad - \quad + \\ \hline -\sqrt{5} \quad \sqrt{5}\end{array}$

$$\begin{aligned}\{x | x \in \mathbb{R}, -\sqrt{5} \leq x \leq \sqrt{5}\} \\[-\sqrt{5}, \sqrt{5}]\end{aligned}$$

l) $x^3 + 3x^2 - 10x < 0$

$x(x^2 + 3x - 10) < 0 \rightarrow x(x+5)(x-2) < 0$

$$\begin{array}{c}- \quad + \quad - \quad + \\ \hline -5 \quad 0 \quad 2\end{array}$$

$$\begin{aligned}\{x | x \in \mathbb{R}, x < -5 \text{ or } 0 < x < 2\} \\(-\infty, -5) \cup (0, 2)\end{aligned}$$

n) $x^3 + 2x^2 - 9x - 18 > 0$

$f(-2) = 0$

$$\begin{aligned}x+2 &\cancel{|} \frac{x^2 + 0x - 9}{x^3 + 2x^2 - 9x - 18} \\&\cancel{|} \frac{x^3 + 2x^2}{0x^2 - 9x} \\&\cancel{|} \frac{0x^2 - 9x}{-9x - 18}\end{aligned}$$

$\begin{array}{c}+ \quad - \quad + \\ \hline -3 \quad -2 \quad 3\end{array}$

$$\{x | x \in \mathbb{R}, -3 < x < 2 \text{ or } x > 3\}$$

$(-3, -2) \cup (3, \infty)$

o) $x^3 - 8 \geq 0$ Quadratic Eqⁿ

$$(x-2)(x^2+2x+4) \quad \sqrt{b^2-4ac}$$

$$(x-2)$$

$\frac{-}{\uparrow}$ No solution

$\{x | x \in \mathbb{R}, x > 2\}$

$(2, \infty)$

2. Solve the inequality

a) $\frac{2x+1}{x^2+1} > 0$ Forever positive

$$2x+1 > 0 \quad x > -\frac{1}{2}$$

$(-\frac{1}{2}, \infty)$

p) $x^9 + x > 0$

$$x(x^8 + 1)$$

$\underbrace{\hspace{1cm}}_{\text{never 0}}$

$\{x | x \in \mathbb{R}, x > 0\}$

$(0, \infty)$

(denominator is an asymptote) but consider sign.

b) $\frac{x+2}{x-3} > 0$

$(-\infty, -2) \cup (3, \infty)$

c) $\frac{x^2+x}{(x-1)^3} < 0$

$$\frac{x(x+1)}{(x-1)^3}$$

$(-\infty, -1) \cup (0, 1)$

d) $\frac{5x}{(x^2-1)^2} < 0$

\uparrow
Forever positive

$(-\infty, -1) \cup (-1, 0)$