

**Section 4.3 – Practice Problems**

1. Find the sum of the interior angles of the polygons for each number of sides.

a) 20  $(n-2)180$

$$\boxed{3240^\circ}$$

b) 17  $(n-2)180$

$$\boxed{2700^\circ}$$

c) 39  $(n-2)180$

$$37 \cdot 180$$

$$\boxed{6660^\circ}$$

d) 23  $(n-2)180$

$$\boxed{3780^\circ}$$

2. One interior angle of a regular polygon is given. Find the number of sides.

a)  $156^\circ$   $\frac{(n-2)180}{n} = 156$

$$156n = 180n - 360$$

$$-24n = -360$$

$$\boxed{n=15}$$

b)  $144^\circ$   $\frac{(n-2)180}{n} = 144$

$$144n = 180n - 360$$

$$-36n = -360$$

$$\rightarrow n = 10$$

c)  $160^\circ$

$$\frac{(n-2)180}{n} = 160$$

$$160n = 180n - 360$$

$$-20n = -360$$

$$\boxed{n=18}$$

d)  $179^\circ$

$$\frac{(n-2)180}{n} = 179$$

$$179n = 180n - 360$$

$$-n = -360$$

$$\boxed{n=360}$$

3. The number of sides of a regular polygon is given. Calculate the measure of each interior angle.

a) 4  $\frac{(n-2)180}{n} = x$   
 $\frac{(4-2)180}{4} = x$   $x = \frac{360}{4}$   $x = 90$

b) 17  $\frac{(n-2)180}{n} = x$   
 $\frac{(17-2)180}{17} = x$   $x = 158.8^\circ$   
 $\frac{15 \cdot 180}{17} = x$

c) 8  $\frac{(n-2)180}{n} = x$   
 $\frac{6 \cdot 180}{8} = x$   $x = 135^\circ$

d) 13  $\frac{(n-2)180}{n} = x$   
 $\frac{11 \cdot 180}{13} = x$   $x = 152.3^\circ$

4. The sum of the interior angles of a regular polygon is given. Calculate the measure of each exterior angle.

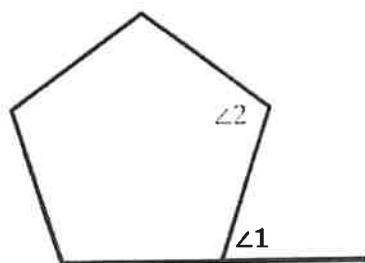
a)  $2880^\circ$   $x = (n-2)180$   
 $2880 = (n-2)180$   
 $16 = n-2$   $n = 18$   
 $\frac{360}{18} = 20$   $20^\circ$

b)  $1620^\circ$   $1620 = (n-2)180$   
 $9 = n-2$   $n = 11$   
 $\frac{360}{11} = 32.72^\circ$

c)  $3780^\circ$   $3780 = (n-2)180$   
 $n = 23$   
 $\frac{360}{23} = 15.7^\circ$

d)  $3420^\circ$   $3420 = (n-2)180$   
 $19 = n-2$   $n = 21$   
 $\frac{360}{21} = 17.1^\circ$

5. Find the missing values for the following polygons.



$\angle 1 = 180 - 108$   
 $= 72^\circ$

$n = 5$   
 $\frac{(n-2)180}{n} = \angle 2$   
 $\angle 2 = \frac{3 \cdot 180}{5}$   
 $\angle 2 = 108^\circ$

$\angle 1 = 72^\circ$   
 $\angle 2 = 108^\circ$

6. If two circles have radii 8 and 12, what is the ratio of the circumferences? Areas?

$$\begin{array}{llll}
 F_s : F_L & P_s : P_L & C_s : C_L & A_s : A_L \\
 8 : 12 & a : b & 2 : 3 & a^2 : b^2 \\
 2 : 3 & 2 : 3 & & 2^2 : 3^2 \Rightarrow 4 : 9 \\
 a : b & & & 
 \end{array}$$

7. If the area of two circles are  $16\pi$  and  $36\pi$ , what is the ratio of the radii? Of the circumferences?

$$\begin{array}{llll}
 A_s : A_L & F_s : F_L & r_s : r_L & C_s : C_L \\
 16\pi : 36\pi & a : b & a : b & a : b \\
 4 : 9 & 2 : 3 & 2 : 3 & 2 : 3 \\
 2^2 : 3^2 & & & \\
 a^2 : b^2 & & & 
 \end{array}$$

8. Two similar cylinders have lateral (sides) surface areas of  $36\pi$  and  $64\pi$ . Find the ratios of their heights.

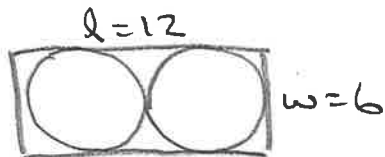
$$\begin{array}{lll}
 A_s : A_L & F_s : F_L & h_s : h_L \\
 36\pi : 64\pi & a : b & a : b \\
 9 : 16 & 3 : 4 & 3 : 4 \\
 3^2 : 4^2 & & \\
 a^2 : b^2 & & 
 \end{array}$$

9. Two spheres of the same density have a surface area of  $16\pi\text{cm}^2$  and  $36\pi\text{cm}^2$ . If the small ball weigh  $6\text{kg}$ , what does the larger sphere weigh?

$$\begin{array}{llll}
 A_s : A_L & F_s : F_L & V_s : V_L & \frac{V_s}{V_L} = \frac{a^3}{b^3} \\
 16\pi : 36\pi & a : b & a^3 : b^3 & \frac{m_s}{m_L} = \frac{a^3}{b^3} \\
 4 : 9 & 2 : 3 & 2^3 : 3^3 & \frac{6\text{kg}}{m_L} = \frac{8}{27} \\
 2^2 : 3^2 & & 8 : 27 & \\
 a^2 : b^2 & & & 
 \end{array}$$

$$m_L = 20.25 \text{ kg}$$

10. Two identical cylinders are tightly packed side by side in a box  $12\text{cm}$  by  $6\text{cm}$  and  $4\text{cm}$  in height. Find the ratio of the volume of the box to the volume of the cylinders.



$$\begin{aligned}
 h &= 4 \text{ cm} \\
 V_{\text{box}} &= lwh \\
 &= 12(6)(4) \\
 &= 288 \text{ cm}^3
 \end{aligned}$$

$$\begin{aligned}
 V_{\text{cyl}} &= \pi r^2 h \\
 &= \pi (3)^2 (4) \\
 &= 36\pi \text{ cm}^2
 \end{aligned}$$

$$V_{\text{two cyl}} = 2(36\pi) = 72\pi \text{ cm}^2$$

$$\begin{aligned}
 \frac{V_{\text{Box}}}{V_{\text{two cyl}}} &= \frac{288}{72\pi} = \frac{4}{\pi} \\
 &= 4 : \pi
 \end{aligned}$$